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(Eds.)



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## IDDM 2020

# The 3rd International Conference on Informatics & Data-Driven Medicine

Proceedings of the 3rd International Conference on Informatics & Data-Driven Medicine

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# Table of Contents

- Preface

Summary: There were 102 papers submitted for peer-review to this workshop. Out of these, 50 papers were accepted for this volume, 31 as regular papers and 18 as short papers.

## Keynote

- Intelligence Science in Digital Healthcare Systems  
*Abdel-Badeeh M. Salem*

## Plenary Session

- Identifying Explosive Epidemiological Cases with Unsupervised Machine Learning 1-10  
*Serge Dolgikh,*
- Information Technology for Early Diagnosis of Pneumonia on Individual Radiographs 11-21  
*Iurii Krak, Olexander Barmak, Pavlo Radiuk*
- Isolation of Tumor Areas of Histological Images for Assessment of Quantitative Parameters 22-28  
*Vassili Kovalev, Valery Malyshev, Artem Piddubnyi, Alona Moskalenko, Anatolii Romaniuk*
- Probabilistic Neuro-Fuzzy System in Medical Diagnostic Task and its Lazy Learning-Selflearning 29-35  
*Yevgeniy Bodyanskiy, Anastasiya Deineko, Iryna Pliss, Olha Chala*
- Methodology of Constructing Statistical Models for Nonlinear Non-stationary Processes in Medical Diagnostic Systems 36-45  
*Peter Bidyuk, Irina Kalinina, Aleksandr Gozhyj*
- Collaborative Deterministic and Stochastic Decision-Making Models in Health Care 46-55  
*Tetiana Shmelova, Abdel-Badeeh M. Salem, Volodymyr Smolanka, Oleksandr Sechko*

## Session 1: Artificial intelligence

- Network Modeling of Coexistence of Virus Strains Admitting Chaotic Behavior 56-61  
*Alexander Nakonechnyi, Vasyl Martsenyuk, Andriy Sverstiuk, Yevhen Davydenko, Igor Andrushchak , Igor Loiko*
- Sequencing for Encoding in Neuroevolutionary Synthesis of Neural Network Models for Medical Diagnosis 62-71  
*Serhii Leoshchenko, Andrii Oliinyk, Sergey Subbotin, Tetiana Zaiko, Serhii Shylo , Viktor Lytvyn*
- On the Modeling Process of Ultrasonic Wave Propagation in a Relaxation Medium by the Three-Point in Time Problem 72-81  
*Zinovii Nytrebych, Volodymyr Il'kiv, Oksana Malanchuk*
- Processing Methods and ECG Signal Recognition Model 82-93  
*Eugene Fedorov, Tetyana Utkina, Kostiantyn Rudakov, Andriy Lukashenko, Ihor Zubko , Michal Greguš ml.*

- Development of a Genetic Method for Image Recognition in the Form of Radiographs  
*Ievgen Fedorchenko, Andrii Oliinyk, Alexander Stepanenko, Tetiana Fedoronchak, Yuliia Fedorchenko, Anastasia Kharchenko, Dmytro Goncharenko* 94-107
- The Use of The Results of Intellectual Monitoring in The Practice of Treatment of Inflammatory Bowel Diseases 108-118  
*Serhii Holub, Andriy Dorofeyev, Gulustan Babayeva, Svitlana Kunitskaya, Oleg Ananiin*
- Modeling of Infectious Disease Dynamics under the Conditions of Spatial Perturbations and Taking into account Impulse Effects 119-128  
*Andrii Bomba, Sergii Baranovsky, Mykola Pasychnyk, Kateryna Malash*
- Specified Diagnosis of Breast Cancer on the basis of Immunogistochemical Images Analysis 129-135  
*Oleh Berezsky, Oleh Pitsun, Tamara Datsko, Bohdan Derysh, Ivan Tsmots, Vasyl Teslyuk*
- On One Nonlinear Mathematical Model of Blood Circulation with the Vessel Walls Reaction within the Hereditary Theory 136-141  
*Petro Pukach, Myroslava Vovk, Yurii Mylyan, Halyna Bilushchak, Pavlo Pukach*
- Decision-Making about Conclusion of Contractual Obligations in the Field of Medical Services 142-148  
*Tetiana Hovorushchenko, Yelyzaveta Hnatchuk, Alla Herts*
- Mathematical Modeling And Processing Of High Resolution Rhythmocardio Signal Based On A Vector Of Stationary And Stationary Related Random Sequences 149-155  
*Petro Onyskiv, Iaroslav Lytvynenko, Serhii Lupenko, Andriy Zozulia*
- Simulation of a Human Operator's Response to Stressors under Production Conditions 156-169  
*Lesia Mochurad, Mariia Yatskiv*
- Mathematical Modeling and Optimization of Technological Parameters of the Obtaining Process of Hydrogel Medical Dressings 170-177  
*Oleksandr Grytsenko, Petro Pukach, Oleh Suberlyak, Ivan Gaydos, Mykola Kushnirchuk, Bohdan Berezhnyy*
- A Computational Approach in the Search of New Biologically Active 9,10-Anthraquinone Derivatives 178-185  
*Maryna Stasevych, Viktor Zvarych, Volodymyr Novikov*
- Mathematical Model Reduction Principle Development 186-196  
*Yaroslav Matviychuk, Nataliia Shakhovska*
- Mathematical Model Building for COVID-19 Diseases Data in European Countries 197-208  
*Maksym Zaliskyi, Roman Odarchenko, Yuliia Petrova, Maksim Iavich, Irakli Pirtskhalava*
- Addressing Medical Diagnostics Issues: Essential Aspects of the PNN-based Approach 209-218  
*Ivan Izonin, Roman Tkachenko, Liliia Ryvak, Khrystyna Zub, Mariia Rashkevych, Olena Pavliuk*
- Recommendation Rules Mining for Reducing the Spread of COVID-19 Cases 219-229  
*Vitaliy Yakovyna, Natalya Shakhovska, Khrystyna Shakhovska, Jaime Campos*
- Application of the Naive Bayesian Classifier in Work on Sentimental Analysis of Medical Data 230-239  
*Nataliya Boyko, Karina Boksho*

- Development of a Markov Model of Changes in Patients' Health Conditions in Medical Projects 240-251  
*Olga Mezentseva, Oleksii Kolesnikov, Katerina Kolesnikova*
- Neural Networks in Intelligent Analysis Medical Data for Decision Support 252-264  
*Vasyl Sheketa, Mykola Pasieka, Nelly Lysenko, Oleksandra Lysenko, Nadia Pasieka, Yulia Romanyshyn*

## Session 2: Information systems in medicine

- The Concept of Developing a Decision Support System for the Epidemic Morbidity Control 265-274  
*Sergiy Yakovlev, Kseniia Bazilevych, Dmytro Chumachenko, Tetyana Chumachenko, Leonid Hulianytskyi, Ievgen Meniailov, Anton Tkachenko*
- Solutions to the 3D Model Problem of Pressure Measurement in the Area of Maxillary Sinus Anastomosis 275-284  
*Alina Nechyporenko, Viktor Reshetnik, Denys Shyian, Victoria Aleksееva, Rادی Radutny, Vitaliy Gargin*
- Designing of Information Model for Prediction of Drug-drug Interactions based on Calculation of Target and Therapeutic Similarity 285-291  
*Olha Marushchak, Rostyslav Kosarevych*
- Mathematical Modeling Covid-19 Wave Structure of Distribution 292-301  
*Kateryna Molodetska, Yuriy Tymonin*
- A Study on Cloud Computing Architectures for Smart Healthcare Services 302-310  
*Dalia Rizk, Hoda Hosny, El-Sayed El-Horbaty, Abdel-Badeeh Salem*
- Translation, Adaptation and Initial Validation of the Food Allergy Quality of Life Questionnaire – Child Form (8 – 12 Years) in Ukrainian Language 311-322  
*Oksana Matsyura, Olena Borysiuk, Lesya Besh, Svitlana Zubchenko, Natalia Lukyanenko, Taras Gutor, Oksana Kovalska, Bertine M. J. Flokstra - de Blok*
- Applying of Information Technologies for Study of the Thyroid Gland Follicular Thyrocytes' Synthetic Activity 323-237  
*Olha Ryabukha, Ivanna Dronyuk*
- Technologies of Object Recognition in Space for Visually Impaired People 338-347  
*Nataliya Boyko, Bohdan Mandych*
- Methodology of Disease Risk Assessment 348-359  
*Karina Melnyk, Natalia Borysova, Svetlana Ershova*
- Variational Formulation of Viscoelastic Problem in Biomaterials with Fractal Structure 360-369  
*Volodymyr Shymanskyi, Yaroslav Sokolovskyy*
- Mathematical Modeling of Diagnosis and Diagnostic Information Space of Chinese Image Medicine for their Unified Representation in Information Systems for Integrative Scientific Medicine 370-376  
*Serhii Lupenko, Oleksandra Orobchuk, Igor Kateryniuk*
- Mathematical Modeling of Rheological Behavior of Anisotropic Biomaterials with Taking Into Account Effects of Memory and Self-organization 377-386  
*Yaroslav Sokolovskyy, Volodymyr Shymanskyi, Maryana Levkovych, Ivan Sokolovskyy, Jaime Campos*
- Information Technology Platform of "Smart" Dental Clinic 387-396  
*Nataliia Kunanets, Volodymyr Pasichnyk, Petro Kravets, Yaroslav Kis, Roksolana Havryliv, Antonii Rzhеuskyi*
- Simulation of Human-Operator Behavior in Solving Intellectual Problems during Control of Technological Processes in Stresses 397-404

*Roman Kaminsky, Natalia Kryvinska*

- Processing of Medical Different Types of Data Using Hadoop and Java MapReduce 405-414  
*Nataliya Boyko, Nazar Tkachuk*
- Medical Content Processing in Intelligent System of District Therapist 415-429  
*Vasyl Lytvyn, Andrii Hryhorovych, Viktor Hryhorovych, Lyubomyr Chyrun, Victoria Vysotska, Myroslava Bublyk*
- Specification of Information Technology for Non Invasive Prediction and Correction of Functional State of Human in Complex Conditions 430-436  
*Bohdan Yavorsky, Myhaylo Bachynskyi*
- Computer Monitoring of Physical and Chemical Parameters of the Environment Using Computer Vision Systems: Problems and Prospects 437-442  
*Yuriy Bashtyk, Jaime Campos, Andriy Fechan, Sviatoslav Konstantyniv, Vitaliy Yakovyna*
- Retrospective Analysis by Multifactor Regression in the Evaluation of the Results of Fine-needle Aspiration Biopsy of Thyroid Nodules 443-447  
*Askold Kucher, Oksana Boyko, Kateryna Ilkanych, Andriy Fechana, Natalya Shakhovska*
- A Two-step Approach in Expert Evaluation of Correctional Information Technologies for Students with Autism Spectrum Disorders 448-457  
*Tetiana Shestakevych, Vasyl Andrunyk*
- The Decision Tree Usage for the Results Analysis of the Psychophysiological Testing 458-472  
*Myroslava Bublyk, Vasyl Lytvyn, Victoria Vysotska, Lyubomyr Chyrun, Yurii Matseliukh, Nataliia Sokulska*
- The Problem of Analysing the Relationships between Individual Characteristics of Individuals with COVID`19 473-482  
*Nataliia Melnykova, Natalya Shakhovska, Volodymyr Melnykov, Mykola Logoyda, Yulia Peleshchak*

# Processing Methods and ECG Signal Recognition Model

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## Abstract

In the work for processing the ECG signal, methods for determining the length of RR interval of ECG signal and calculating on its basis the boundaries of RR interval of ECG signal, geometric converting of RR intervals of ECG signal have been proposed. The proposed definition of the length of RR interval of ECG signal uses statistical estimation of local maximum and band-pass filtering, which decreases the computational complexity, and decreases the dependence on noise and permit to use dynamic threshold, which increases the accuracy of calculating the length and boundaries of RR intervals of ECG signal. The proposed geometric converting of RR intervals of ECG signal makes it possible to convert RR intervals to a unified amplitude-time window, which permits to form samples of ECG signal on basis its structure. The proposed model of ECG signal recognition is based on adaptive probabilistic neural network that allows identification of the structure and parameters, which increases the recognition probability. The proposed method for identifying the structure and parameters of the model for recognizing ECG signal samples is based on adaptive clustering, which provides a high degree of compression and clustering of ECG signal samples. To evaluate the proposed methods and model, quality criteria are determined. Numerical studies, which allow to evaluate the proposed methods and model, have been carried out. The proposed methods and model make it possible to formulate and solve the problems of structuring, transforming and recognizing the ECG signal, which is used for ECG diagnostics.

## Keywords 1

ECG diagnostics, ECG signal structuring, calculation of length of RR interval, determination of boundaries of RR intervals, geometric transformation of RR intervals, adaptive probabilistic neural network, identification of structure and parameters of model for recognizing ECG signal patterns

## 1. Introduction

Automated medical diagnostics of a person means decision making based on the analysis of a digital signal, which increases the quality of diagnostics of the person under study. In contrast to the traditional approach, computer medical diagnostics accelerates and increases the accuracy of the identification process, which is critical in case of limited time.

A important class of medical diagnostics of a person is formed by methods based on the recognition of electrocardiograms (ECG) [[1], [2], [3], [4]].

To analyze the ECG signal, traditional speech recognition methods, such as:

- dynamic programming [[5], [6]];

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- vector quantization [[7], [8]];
- artificial neural networks [[9], [10]];
- decision tree [[11], [12]];
- a combination of these methods [[13]],

can be used, which, when identifying a signal, split it into frames (have the same length) without analyzing its structure, which decrease the efficiency of ECG diagnostics.

The highest probability of ECG signal recognition is achieved by means of neural networks.

Currently, the following artificial neural networks are commonly used to recognize ECG signals:

- multilayer perceptron (MLP) [[14], [15]],
- neural network based on radial basis functions (RBFNN) [[16], [17]];
- probabilistic neural network (PNN) [[18], [19]]
- support vector machine (SVM) [[20], [21]];
- self-organizing feature map (SOM) [[22], [23]].

These artificial neural networks have next disadvantages:

- there is no automatic calculation of the number of hidden layers;
- there is no automatic calculation of the number of neurons in hidden layers;
- it is required to store all training patterns;
- possess a high computational complexity of learning;
- do not have a high recognition probability;
- methods of local search are used for training, which can lead to falling into a local extremum.

In this regard, it is relevant to choose a model and create a method for identifying its structure and parameters, which will eliminate the indicated disadvantages.

The structuring of ECG signal is based on the division of ECG signal based on the length of RR interval.

To determine the length of RR interval, traditional methods for calculation the fundamental tone of a person, such as [[24], [25]]:

- wavelet-spectral (amplitude-time-frequency) methods;
- amplitude-time methods;
- cepstral (amplitude-frequency) methods;
- spectral (amplitude-frequency) methods;

These methods have next disadvantages:

- do not use dynamic threshold, which increases the accuracy of calculating the length of RR interval.
- possess a high computational complexity;
- depend on noise level, which decreases the accuracy of calculating the length of RR interval;

In this regard, it is relevant to develop a method for structuring the ECG signal, which will eliminate the indicated disadvantages.

As geometric transformations of ECG signal, scaling and shifting are usually used.

To scale a discrete ECG signal, a transition to a continuous one by interpolation with subsequent sampling of scaled ECG signal is usually used.

In this regard, it is relevant to create processing methods and ECG signal recognition model, which will eliminate the indicated disadvantages.

The goal of the article is to increase the efficiency of ECG diagnostics due to processing methods and ECG signal recognition model.

To reach this goal, it is necessary to solve the next tasks:

1. Creation of a method for structuring and transforming an ECG signal.
2. Determination of quality criterion of ECG signal structuring.
3. Selection of a model for recognizing ECG signal patterns.
4. Determination of quality criterion for recognizing ECG signal patterns.
5. Development of a method for identifying the structure and parameters of the model for recognizing ECG signal patterns.
6. Determination of characteristics and quality criterion of identification of the structure and parameters of the model for recognizing ECG signal patterns.

## 2. Method of structuring and transforming the ECG signal

Training sample formation method includes:

1. Calculation of the length of RR interval based on statistical estimation of local maximum and band-pass filtering.
2. Calculation of the boundaries of RR intervals based on the fundamental tone.
3. Geometric converting of RR intervals to a unified amplitude-time window.

### 2.1. Determination of the length of RR interval of ECG signal based on statistical estimation of local maximum and band-pass filtering

The article proposes a method for calculating the length of RR interval of ECG signal based on statistical estimation of local maximum and band-pass filtering, which includes the next steps:

1. Set ECG signal  $y(h)$ ,  $h \in \overline{1, H^f}$ . Set the lower cutoff frequency in Hz  $f1$ ,  $f1=5$ . Set filtering parameter  $\alpha$ ,  $0 < \alpha < 1$ . Set the upper cutoff frequency in Hz  $f2$ ,  $f2=35$ . Set the number of windows in length  $H$ ,  $H = 2^b$ , where the parameter  $b$  is selected from the condition  $b-1 < \log_2(f_d/f_{\min}) < b$ ,  $f_d$  is the sampling frequency of ECG signal in Hz,  $f_{\min}$  is the minimum frequency of R wave in Hz (for  $f_d = 360$ ,  $f_{\min} = 5$ ),  $[\cdot]$  is the integer part.

2. Divide ECG signal into windows:

$$s_i(h) = y((i-1) \cdot H + h + 1), \quad h \in \overline{0, H-1}, \quad i \in \overline{1, I}.$$

3. Preprocessing of windows using a low-pass filter:

$$\tilde{s}_i(h) = s_i(h+1) - \alpha s_i(h), \quad h \in \overline{0, H-1}, \quad i \in \overline{1, I}.$$

4. Determinate the spectrum of weighted windows using weighting with Hamming window and forward discrete Fourier transform:

$$\begin{aligned} \hat{s}_i(h) &= \tilde{s}_i(h)w(h), \quad h \in \overline{0, H-1}, \quad i \in \overline{1, I}, \\ \hat{S}_i(l) &= \sum_{h=0}^{H-1} \hat{s}_i(h)e^{-j(2\pi/H)lh}, \quad l \in \overline{0, H-1}, \quad i \in \overline{1, I}, \\ \tilde{S}_i(l) &= \begin{cases} \hat{S}_i(l), & \frac{f1 \cdot H}{f_d} \leq l \leq \frac{f2 \cdot H}{f}, \\ 0, & \frac{f1 \cdot H}{f_d} > l \vee l > \frac{f2 \cdot H}{f}, \end{cases} \\ & \quad l \in \overline{0, H-1}, \quad i \in \overline{1, I}, \\ w(h) &= 0.54 + 0.46 \cdot \cos \frac{2\pi h}{H}, \end{aligned}$$

where  $w(h)$  is the Hamming window.

5. Compute the inverse discrete Fourier transform of filtered windows:

$$\tilde{s}_i(h) = \text{Re} \left( \frac{1}{H} \sum_{l=0}^{H-1} \tilde{S}_i(l) e^{j(2\pi/H)lh} \right), \quad h \in \overline{0, H-1}, \quad i \in \overline{1, I}.$$

6. Combine filtered windows into ECG signal:

$$\tilde{y}((i-1) \cdot H + h + 1) = \tilde{s}_i(h), \quad h \in \overline{0, H-1}, \quad i \in \overline{1, I}.$$

7. Determinate the positions of local maximum in the filtered R segment.

7.1. Set the sample index  $h=1$ . Set the count of local maximum  $Q=0$ .

7.2. If  $\tilde{y}(h) > \tilde{y}(h-1) \wedge \tilde{y}(h) > \tilde{y}(h+1) \wedge \tilde{y}(h) > 0$ , then fix the point of the local maximum, i.e.  $e_{Q+1} = h$ , increase the count of local maximum, i.e.  $Q = Q+1$ .

7.3. If  $h < H^r - 1$ , then go to the next sample, i.e.  $h = h+1$ , go to step 7.2.

8. Determinate distances between local maximum in the filtered R segment

$$\Delta_n = e_{n+1} - e_n, \quad n \in \overline{1, Q-1}.$$

9. Determinate mean of distances:

$$\mu = \frac{1}{Q-1} \sum_{n=1}^{Q-1} \Delta_n.$$

10. Determinate standard deviation of distances:

$$\sigma = \sqrt{\frac{1}{Q-1} \sum_{n=1}^{Q-1} (\Delta_n)^2 - \mu^2}.$$

11. Delete outliers from distances.

11.1. Set the count of new distances  $\tilde{Q} = 0$ . Set distance index  $n = 1$ .

11.2. If  $\mu - \sigma \leq \Delta_n \leq \mu + \sigma$ , then fix a new distance ( $\tilde{\Delta}_{\tilde{Q}+1} = \Delta_n$ ), increase the count of new distances ( $\tilde{Q} = \tilde{Q} + 1$ ).

11.3. If  $n < Q - 1$ , then go to the following distance, i.e.  $n = n + 1$ , go to step 11.2.

12. Determinate the length of RR interval as a mean of new distances:

$$N^{FT} = \frac{1}{\tilde{Q}} \sum_{n=1}^{\tilde{Q}} \tilde{\Delta}_n.$$

As a result, the length of RR interval is determined.

## 2.2. Determination of the boundaries of RR intervals of ECG signal

The author's method for calculating the boundaries of RR interval of ECG signal includes the following steps:

1. Set ECG signal  $y(h)$ ,  $h \in \overline{1, H^f}$ . Set the parameter  $\gamma$  for determining the boundaries of RR intervals of ECG signal,  $0 < \gamma < 1$ . Set the length of RR interval of ECG signal.

2. Initialize the variables to determine the boundaries of RR intervals of ECG signal in the form:

$$H_0^{\max} = \arg \max_h y(h), \quad h \in \{1, \dots, \gamma H_0^{FT}\},$$

$$H_0^{FT} = H^{FT}.$$

3. Set the count of RR interval of ECG signal  $I = 1$ .

4. Calculating the boundaries of RR interval of ECG signal in the form:

$$H_I^{\min} = H_{I-1}^{\max},$$

$$H_I^{\max} = \arg \max_h y(h), \quad h \in \{H_I^{\min} + (1 - \gamma) \cdot H_{I-1}^{FT}, \dots, H_I^{\min} + (1 + \gamma) \cdot H_{I-1}^{FT}\},$$

$$H_I^{FT} = H_I^{\max} - H_I^{\min}.$$

5. If  $H_I^{\max} \leq H^f$ , then increase the count of quasiperiodic fluctuations, i.e.  $I = I + 1$ , go to step 4.

Set of boundaries of quasiperiodic segment fluctuations are formed.

## 2.3. Geometric transformation of RR intervals of ECG signal to a unified amplitude-time window

The paper proposes a method of geometric transformation of RR intervals of ECG signal to a unified amplitude-time window, which consist the next steps:

1. Set ECG signal  $y(h)$ ,  $h \in \overline{1, H^f}$ . Set the count of quantization levels of ECG signal  $L$  (for an 11-bit pattern  $L = 2048$ ) and set of boundaries of RR intervals of ECG signal  $\{(H_i^{\min}, H_i^{\max})\}$ ,

$i \in \overline{1, I}$ , where  $I$  is the count of patterns. Set the length of the amplitude-time window  $H$ ,  $H = 2^b$ , where the parameter  $b$  is selected from the condition  $b-1 < \log_2(f_d/f_{\min}) < b$ ,  $f_d$  is the sampling frequency of ECG signal in Hz,  $f_{\min}$  is the minimum frequency of R wave in Hz (for  $f_d = 360$ ,  $f_{\min} = 5$ ).

2. Calculate the maximum and minimum values of the transformation of RR intervals of ECG signal in the form:

$$A_i^{\max} = \max_h y(h), \quad h \in \{H_i^{\min}, \dots, H_i^{\max}\},$$

$$A_i^{\min} = \min_h y(h), \quad h \in \{H_i^{\min}, \dots, H_i^{\max}\}.$$

3. Calculate a finite family of discrete patterns shifted in amplitude and time, defined by a finite set of integers bounded finite discrete functions  $X^s = \{x_i^s \mid i \in \{1, \dots, I\}\}$ , in the form:

$$x_i^s(h) = \begin{cases} y(h + N_i^{\min} - 1) - A_i^{\min}, & h \in \{1, \dots, H_i + 1\}, \\ 0, & h \notin \{1, \dots, H_i + 1\}, \end{cases}$$

$$H_i = H_i^{\max} - H_i^{\min},$$

$$A_i = A_i^{\max} - A_i^{\min}.$$

4. Calculate a finite family of continuous patterns obtained as a result of interpolation and defined by a finite set of real-valued bounded finite continuous functions  $\Psi = \{\psi_i \mid i \in \{1, \dots, I\}\}$  in the form:

$$\psi_i(t) = \begin{cases} \sum_{h=1}^{H_i} \chi_{(t_h, t_{h+1})}(t) \left( x_i^s(h) + \frac{x_i^s(h+1) - x_i^s(h)}{\Delta t} (t - t_h) \right) + \sum_{h=1}^{H_i+1} \chi_{\{t_h\}}(t) x_i^s(h), & \forall t \in [\tilde{T}^{\min}, \tilde{T}^{\max}], \\ 0, & \forall t \notin [\tilde{T}^{\min}, \tilde{T}^{\max}], \end{cases}$$

$$\tilde{T}^{\min} = \Delta t, \quad \tilde{T}^{\max} = 2^b \Delta t, \quad t_n = h \Delta t,$$

$$\chi_B(t) = \begin{cases} 1, & t \in B, \\ 0, & t \notin B, \end{cases}$$

where  $\Delta t$  is the quantization step by time of ECG signal,  $\chi_B(t)$  is the indicator function.

5. Calculate a finite family of time-scaled and time-shifted continuous patterns defined by a finite set of real-valued bounded finite continuous functions  $\Psi^s = \{\psi_i^s \mid i \in \{1, \dots, I\}\}$  in the form:

$$\psi_i^s(t) = \begin{cases} \psi_i \left( T_i \frac{t - \tilde{T}^{\min}}{\tilde{T}^{\max} - \tilde{T}^{\min}} \right), & \forall t \in [\tilde{T}^{\min}, \tilde{T}^{\max}], \\ 0, & \forall t \notin [\tilde{T}^{\min}, \tilde{T}^{\max}], \end{cases}$$

$$\tilde{T}^{\min} = \Delta t, \quad \tilde{T}^{\max} = 2^b \Delta t.$$

6. Calculate a finite family of amplitude-scaled and amplitude-shifted continuous patterns defined by a finite set of real-valued bounded finite continuous functions  $\Psi^{ss} = \{\psi_i^{ss} \mid i \in \{1, \dots, I\}\}$  in the form:

$$\psi_i^{ss}(t) = \begin{cases} \tilde{A}^{\min} + \frac{\tilde{A}^{\max} - \tilde{A}^{\min}}{\tilde{A}_i^{\max} - \tilde{A}_i^{\min}} \psi_i^s(t), & \forall t \in [\tilde{T}^{\min}, \tilde{T}^{\max}], \\ 0, & \forall t \notin [\tilde{T}^{\min}, \tilde{T}^{\max}], \end{cases}$$

$$\tilde{A}_i^{\max} = \max_t \psi_i^s(t), \quad t \in [\tilde{T}^{\min}, \tilde{T}^{\max}],$$

$$\tilde{A}_i^{\min} = \min_t \psi_i^s(t), \quad t \in [\tilde{T}^{\min}, \tilde{T}^{\max}],$$

$$\tilde{A}^{\min} = 1, \quad \tilde{A}^{\max} = L.$$

7. Calculate a finite family of discrete patterns converted from continuous patterns by sampling in time and defined by a finite set of integer bounded finite discrete functions  $S = \{s_i \mid i \in \{1, \dots, I\}\}$  in the form:

$$s_i(h) = \text{round}(\psi_i^{ss}(h\Delta t)), \quad h \in \{\tilde{N}_i^{\min}, \dots, \tilde{N}_i^{\max}\},$$

$$\tilde{N}_i^{\min} = \tilde{T}_i^{\min} / \Delta t, \quad \tilde{N}_i^{\max} = \tilde{T}_i^{\max} / \Delta t,$$

where  $\text{round}()$  is the function that rounds to the nearest integer.

Set of ECG signal patterns, which are located in a unified amplitude-time window, are formed.

### 3. Determination of quality criterion for ECG signal structuring

The work formulates the following quality criterion for ECG signal structuring, which means the choice of such a parameter  $\gamma$  that will deliver the minimum of the root-mean-square error:

$$F = \frac{1}{2I} \sum_{i=1}^I (\tilde{N}_i^{\min} - N_i^{\min})^2 + (\tilde{N}_i^{\max} - N_i^{\max})^2 \rightarrow \max_{\gamma}, \quad (1)$$

where  $\tilde{N}_i^{\min}, \tilde{N}_i^{\max}$  are the boundaries of RR intervals of ECG signal set by the expert,  $N_i^{\min}, N_i^{\max}$  – calculated boundaries of RR intervals of ECG signal.

### 4. Model for recognizing ECG signal patterns

Adaptive probabilistic neural network (APNN) based on multidimensional Gaussian functions is proposed as a model for recognizing ECG signal patterns, which allows identification of the structure and parameters and is defined in the following form:

$$y_j = \frac{1}{n_j} \sum_{i=1}^K I(z_i - j) G_i(\mathbf{x}), \quad j \in \overline{1, N^{out}},$$

$$G_i(\mathbf{x}) = \frac{1}{\sqrt{(2\pi)^N \det \mathbf{C}_i}} \exp\left(-\frac{1}{2}(\mathbf{x} - \mathbf{m}_i)^T \mathbf{C}_i^{-1}(\mathbf{x} - \mathbf{m}_i)\right),$$

$$\mathbf{C}_i = \text{diag}(\sigma_{i1}^2, \dots, \sigma_{iN}^2),$$

$$\det \mathbf{C}_i = \prod_{k=1}^N \sigma_{ik}^2,$$

$$n_j = \sum_{i=1}^K I(z_i - j),$$

$$I(a) = \begin{cases} 1, & a = 0, \\ 0, & \text{else,} \end{cases}$$

where  $w_{ij}$  are the weights,  $\mathbf{m}_i$  is the vector of mathematical expectations of the  $N$  dimension of the  $i$ -th Gaussian function,  $\mathbf{C}_i$  is the diagonal covariance matrix of the  $N \times N$  dimension of the  $i$ -th Gaussian function,  $N$  is a pattern length,  $K$  is the number of Gaussian functions,  $N^{out}$  is the number of classes of RR interval,  $z_i$  is a marker of the class of RR interval of the  $i$ -th Gaussian function,  $z_i \in \{1, \dots, N^{out}\}$ .

### 5. Determination of quality criterion for recognizing ECG signal patterns

The work formulates the following quality criterion for recognizing ECG signal patterns, which means the choice of such a set of parameters  $\Theta = \{w_{ij}, \mathbf{m}_i, \mathbf{C}_i\}$ , that will deliver the maximum recognition probability:

$$F = \frac{1}{I} \sum_{\mu=1}^I I(\max_j y_{\mu j} - \max_j d_{\mu j}) \rightarrow \max_{\ominus}, j \in \overline{1, N^{out}}, \quad (2)$$

$$I(a) = \begin{cases} 1, & a = 0, \\ 0, & \text{else,} \end{cases}$$

where  $\mathbf{d}_{\mu}$  is a binary vector, which is set by the expert for the  $\mu$ -th pattern and corresponds to the number of the class of RR interval,  $\mathbf{y}_{\mu}$  is a real vector, which is calculated by the model for the  $\mu$ -th pattern and corresponds to the number of the class of RR interval.

## 6. Method for identifying the structure and parameters of the model for recognizing ECG signal patterns

Determination of the number of Gaussian functions of APNN is not automated and is performed by an operator based on his empirical experience. Therefore, in order to calculate the count and parameters of APNN, a clustering method with adaptive count of clusters (corresponding to Gaussian functions) is proposed, while the center of the first cluster is selected as a pattern of RR interval with a minimum distance to the remaining patterns. The author's adaptive clustering method includes the following steps:

1. Set a set of patterns of RR interval  $S = \{s_i(n)\}$ ,  $i \in \overline{1, I}, n \in \overline{1, N}$ , which are in a unified amplitude-time window with length  $N$  and height  $L$ , where  $I$  is the count of patterns. Set a set of markers of classes of RR interval  $Q = \{q_i\}$ ,  $q_i \in \{1, \dots, N^{out}\}$ ,  $q_i \leftrightarrow s_i$ ,  $i \in \overline{1, I}$ ,  $N^{out}$  is the count of classes of RR interval. Set the initial value of the parameter  $\varepsilon$ ,  $0 < \varepsilon < 1$ . Set step  $\Delta\varepsilon$ ,  $0 < \Delta\varepsilon < 1$ .
2. Calculate the normalized square of the distance between each pair of patterns of RR interval

$$D_{ij} = \frac{\|s_i - s_j\|^2}{NL^2}, i \in \overline{1, I}, j \in \overline{1, I}.$$

3. Calculate the distance between each pattern of RR interval and set of patterns of RR interval

$$d_i = \sum_{j=1}^I D_{ij}, i \in \overline{1, I}.$$

4. Determine the number of pattern of RR interval with the minimum distance

$$i^* = \arg \min_i d_i, i \in \overline{1, I}.$$

5. Set the pattern of RR interval with the minimum distance as a center of the first cluster ( $\mathbf{m}_1 = \mathbf{s}_{i^*}$ ), set the zero matrix as the diagonal covariance matrix of the first cluster ( $\mathbf{C}_1 = \mathbf{0}$ ), set the count of patterns of RR interval in the first cluster to one, i.e.  $a_1 = 1$ , set the marker of the class of RR interval pattern with the minimum distance as a marker of the first cluster, i.e.  $z_1 = q_{i^*}$ .

6. Set the count of clusters  $K = 1$ .

7. Set the count of pattern of RR interval  $i = 1$ .

8. If  $i^* = i$ , then go to step 15.

9. Calculate the normalized square of the distance between the  $i$ -th pattern of RR interval and centers of clusters

$$D_k = \frac{\|s_i - \mathbf{m}_k\|^2}{NL^2}, k \in \overline{1, K}.$$

10. Calculate the smallest normalized square of the distance between the  $i$ -th pattern of RR interval and centers of clusters

$$d^* = \min_k D_k, k \in \overline{1, K}.$$

11. Determine the count of the cluster with the minimum distance

$$k^* = \arg \min_k D_k, k \in \overline{1, K}.$$

12. If  $d^* \leq \varepsilon$  and  $z_{k^*} = q_i$ , then calculate a new center of the  $k^*$ -th cluster, i.e.

$\mathbf{m}_{k^*} = \frac{a_{k^*} \mathbf{m}_{k^*} + \mathbf{s}_i}{a_{k^*} + 1}$ , calculate a new diagonal covariance matrix of the  $k^*$ -th cluster, i.e.

$\mathbf{C}_{k^*} = \text{diag}(\sigma_{k^*}^2)$ ,  $\sigma_{k^*}^2 = \frac{a_{k^*} \sigma_{k^*}^2 + (\mathbf{s}_i - \mathbf{m}_{k^*})(\mathbf{s}_i - \mathbf{m}_{k^*})^T}{a_{k^*} + 1}$ , increase the count of patterns of RR interval

in the  $k^*$ -th cluster, i.e.  $a_{k^*} = a_{k^*} + 1$ .

13. If  $d^* > \varepsilon$ , then set the  $i$ -th pattern as the center of a new cluster; i.e.  $\mathbf{m}_{K+1} = \mathbf{s}_i$ , set the zero matrix as a diagonal covariance matrix of a new cluster, i.e.  $\mathbf{C}_{K+1} = \mathbf{0}$ , set the count of patterns of RR interval in the new cluster to one  $a_{K+1} = 1$ , set the marker of the class of the  $i$ -th pattern as the marker of a new cluster, i.e.  $z_{K+1} = q_i$ , increase the count of clusters, i.e.  $K = K + 1$ .

14. If  $d^* \leq \varepsilon$  and  $z_{k^*} \neq q_i$ , then decrease the value of  $\varepsilon$  parameter, i.e.  $\varepsilon = \varepsilon - \Delta\varepsilon$ , go to step 6.

15. If  $i < I$ , then go to a new pattern ( $i = i + 1$ ), go to step 8.

The count, parameters and markers of cluster classes, which correspond to the Gaussian functions of APNN, are determined.

## 7. Determination of characteristics and quality criterion of identification of the structure and parameters of the model for recognizing ECG signal patterns

To evaluate the clustering method, which makes it possible to calculate the count and parameters of radial basis functions of APNN, the following characteristics are used in the work:

1. The probability of false clustering means the ratio of the count of clusters that contain patterns of different classes to the total count of clusters

$$P = \frac{V}{K},$$

where  $V$  is the count of clusters that contain patterns of different classes,  $K$  is the total count of clusters.

2. Compression ratio

$$C = \frac{I}{K},$$

where  $I$  is the count of patterns,  $K$  is the total count of clusters.

Based on the probability of false clustering and the compression ratio, the following criterion for the quality of clustering:

$$F = P + \frac{1}{C} \rightarrow \min_{\varepsilon}, \quad (3)$$

is formulated, which means the choice of such a value  $\varepsilon$  that gives the minimum to the sum of the clustering probability and the reciprocal of the compression ratio.

## 8. Numerical study of the method for structuring and transforming the ECG signal

For ECG signals, the sampling frequency  $f_d = 360\text{Hz}$ , the count of quantization levels  $L = 2048$  were set. Window length  $N = 512$ .

As a result of a numerical research of the method for ECG signal structuring with the parameter  $\gamma = 0.5$  for ECG signals of the people from the MIT-BIH Arrhythmia database, according to criterion (1), a root-mean-square error of 0.02 was calculated.

Figs. 1-3 show an initial ECG signal (Fig. 1) with the definition of the boundaries of RR intervals of ECG signal (Fig. 2) and geometric converts of RR intervals of ECG signal to a unified amplitude-time window (Fig. 3).

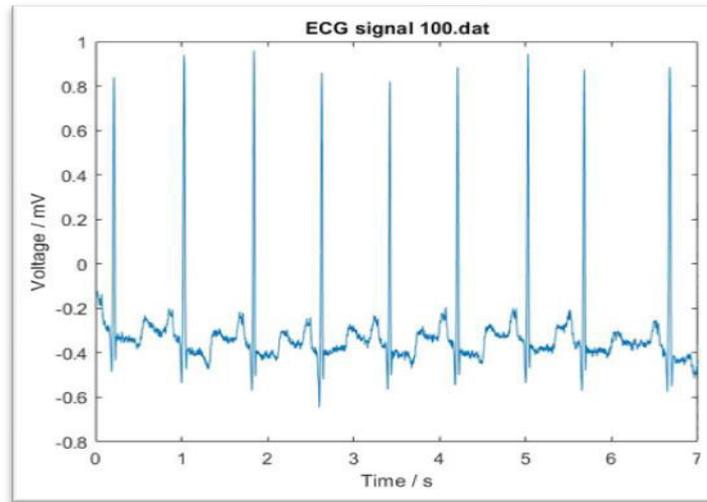


Figure 1: Initial ECG signal (11-bit, 360 Hz, length 2521).

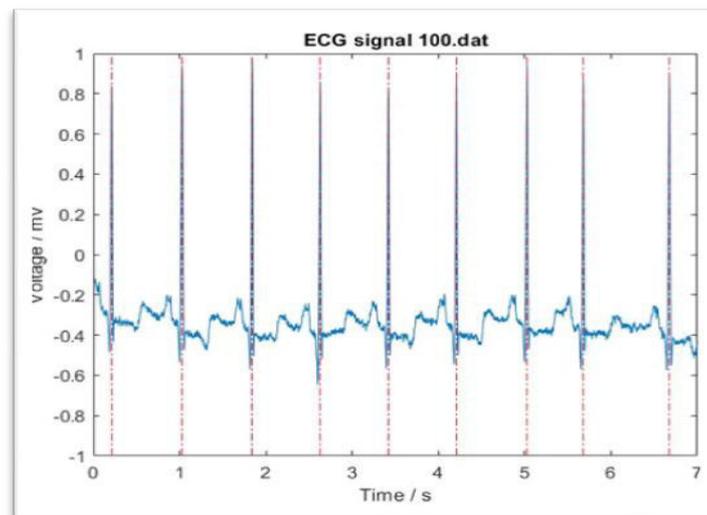


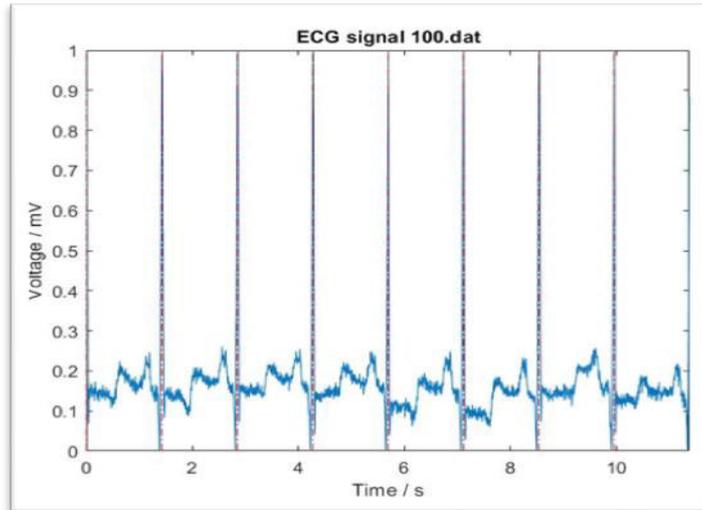
Figure 2: ECG signal after marking the boundaries of RR intervals (parameter  $\gamma = 0.5$ ).

## 9. Numerical research of the method for identifying the structure and parameters of the model for recognizing ECG signal patterns

For ECG signals, the sampling frequency  $f_d = 360\text{Hz}$ , the count of quantization levels  $L = 2048$  were set. Window length  $N = 512$ .

As a result of a numerical research of the clustering method, which allows to determine the number, parameters and markers of classes of Gaussian functions of APNN, with the parameter  $\varepsilon = 0.001$  for ECG signals of the people from the MIT-BIH Arrhythmia database, according to criterion (3), the compression ratio of  $C = 2$  and the probability of false clustering  $P = 0$  were obtained.

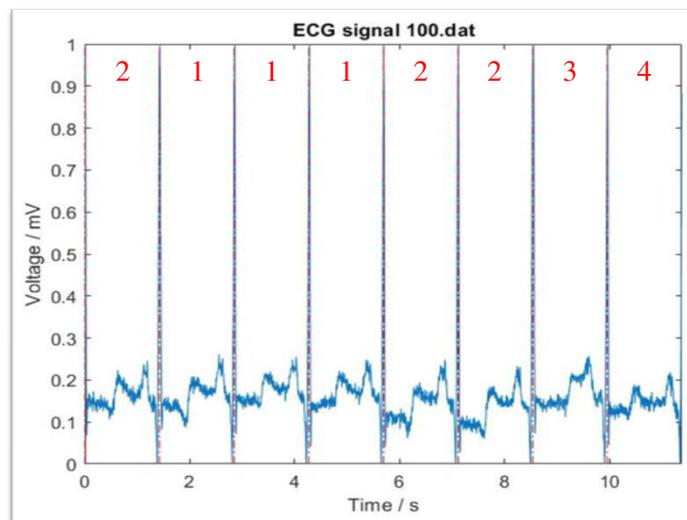
Fig. 4 shows an example of a previously structured ECG signal marked with cluster numbers (Fig. 3). In this case, the clusters with numbers 1, 2, 3 correspond to one class (normal heartbeat), and the cluster with number 4 corresponds to another class (atrial premature heartbeat), i.e.  $z_1 = \{1, 2, 3\}$ ,  $z_2 = \{4\}$ .



**Figure 3:** ECG signal after geometric converts of RR intervals to a unified amplitude-time window.

## 10. Numerical study of the model for recognizing ECG signal patterns

Table 1 shows the probabilities of recognizing ECG signal patterns obtained on the basis of the MIT-BIH Arrhythmia based on artificial neural networks according to criterion (2). At the same time, multilayer perceptron had 2 hidden layers (each consisted of 512 neurons, like the input layer), and the neural network based on radial basis functions had one hidden layer (consisted of 1024 neurons, like the input layer).



**Figure 4:** ECG signal after clustering (parameter  $\varepsilon = 0.001$ ).

**Table 1**  
Probability of recognition of ECG signal patterns

Artificial neural network	Recognition probability
Multilayer perceptron	0.80
Neural network based on radial basis functions	0.85
Support vector machine	0.9
<b>Proposed adaptive probabilistic neural network</b>	<b>0.98</b>

According to Table 1, the proposed adaptive probabilistic neural network gives the best results.

## 11. Conclusions

1. To solve the problem of increasing the quality of ECG diagnostics, the corresponding methods of ECG signal pre-processing, such as calculation of the length of RR interval and signal transformation, as well as methods for identifying the structure and parameters of the model for recognizing RR intervals of ECG signal have been investigated.
2. A method for structuring and transforming an ECG signal has been proposed, which consists: calculation of the length of RR interval of ECG signal based on statistical estimation of local maximum and band-pass filtering, which decreases the computational complexity and decreases the dependence on noise and permits to use dynamic threshold, which increases the accuracy of calculating the length and boundaries of RR intervals; geometric transformation of RR interval of ECG signal, which makes it possible to transform RR intervals to a unified amplitude-time window, which permits to form patterns of ECG signal on basis its structure.
3. A model for recognizing an ECG signal based on adaptive probabilistic neural network, which allows identification of the structure and parameters, is proposed, which increases the recognition probability.
4. A method for determining the structure and parameters of the model for recognizing ECG signal patterns, which is based on adaptive clustering, is proposed, which provides a high degree of compression and clustering of ECG signal patterns.
5. A numerical study of the method of structuring and transforming the ECG signal, which allowing to evaluate the proposed method, has been carried out.
6. A numerical research of the method for identifying the structure and parameters of the model for recognizing ECG signal patterns, which allows to evaluate the proposed method, has been carried out.
7. A numerical research of the model for recognizing ECG signal patterns, which makes it possible to evaluate the efficiency of the proposed model (the recognition probability has increased to 0.98), has been carried out.
8. The proposed methods and model make it possible to formulate and solve the problems of structuring, transforming and recognizing the ECG signal, which is used for ECG diagnostics.

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